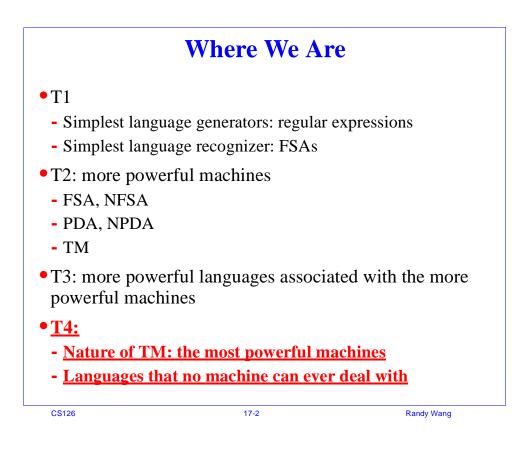
CS 126 Lecture T4: Computability

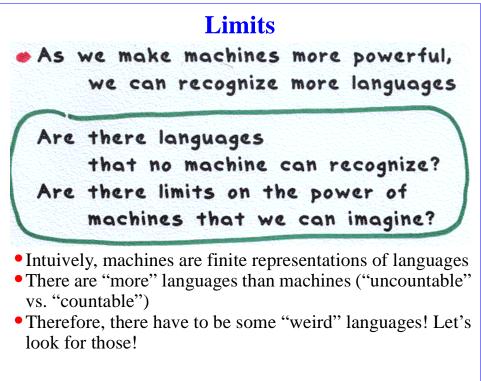
Outline

• Introduction

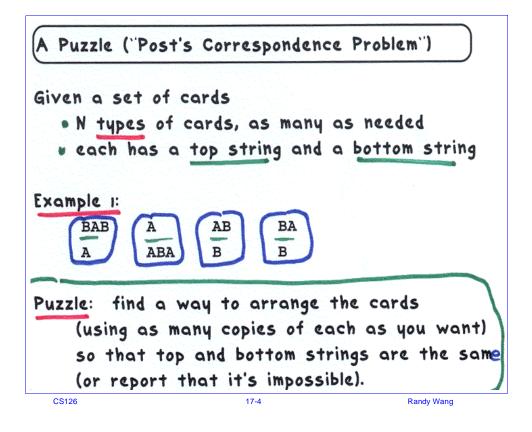
- Nature of Turing machines
- Uncomputability
- Conclusions

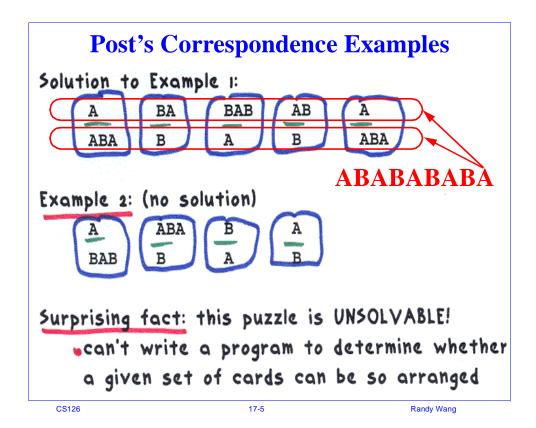
CS126

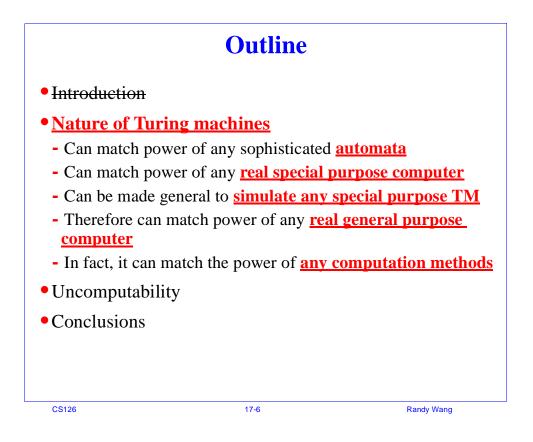


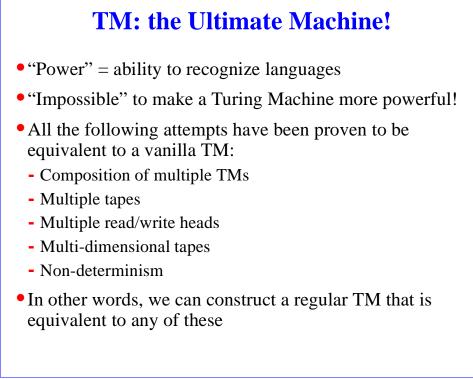


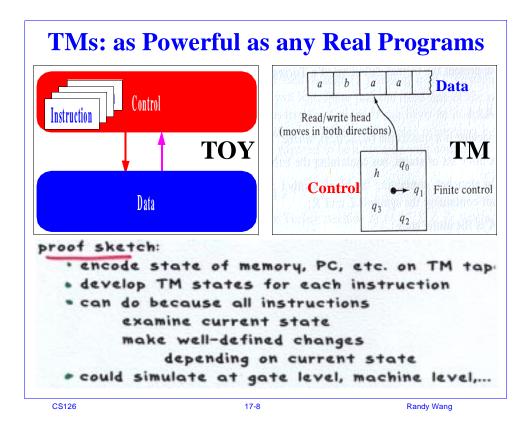
Randy Wang

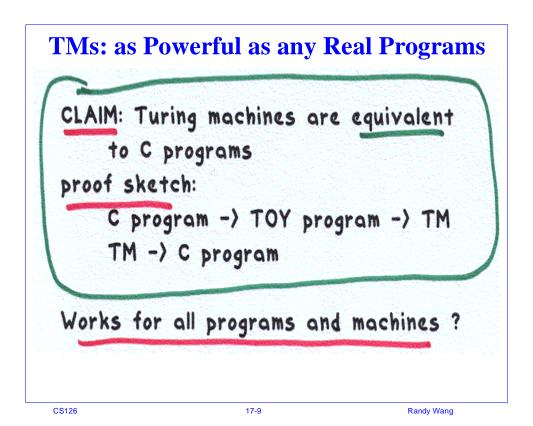


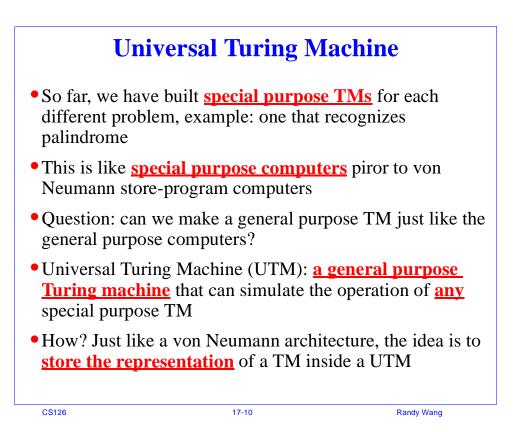


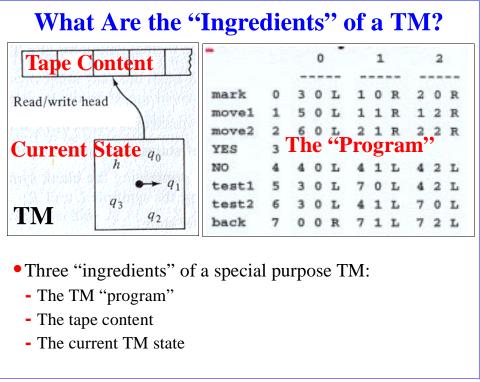




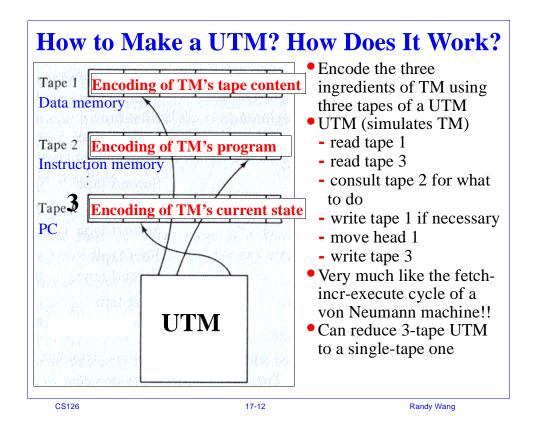


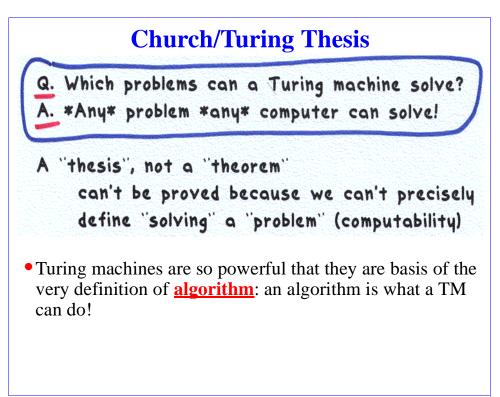


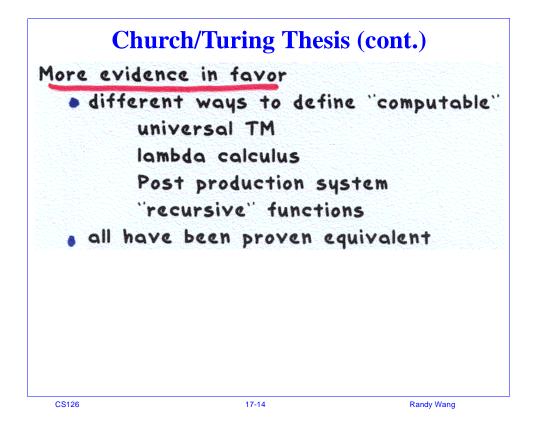


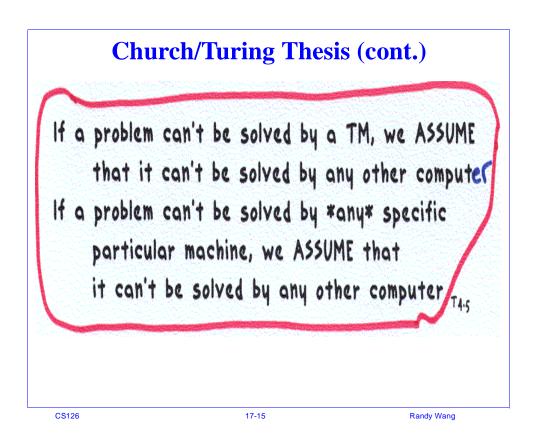


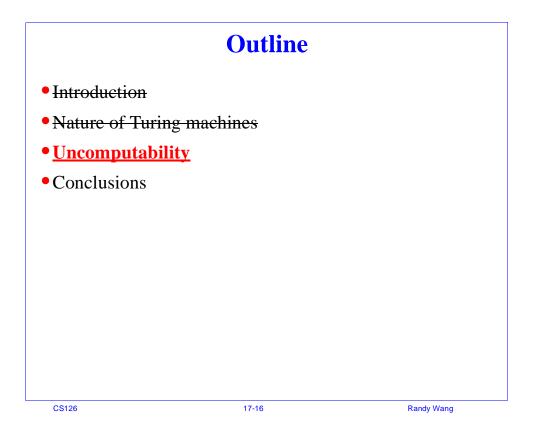
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Randy Wang
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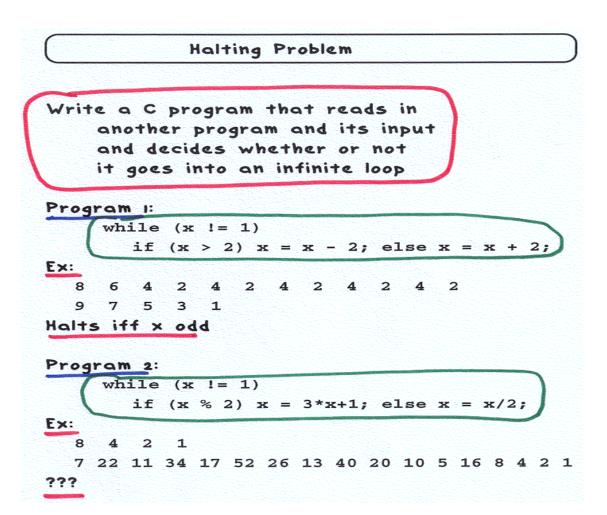


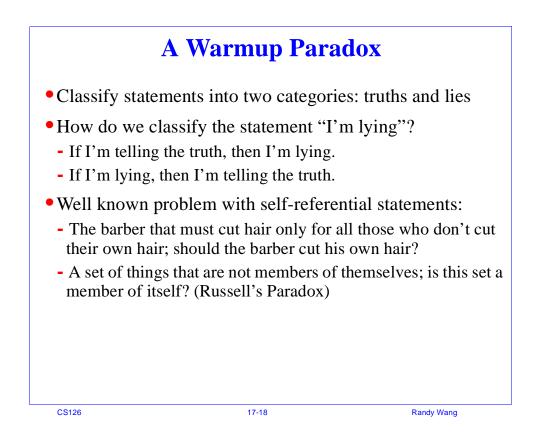


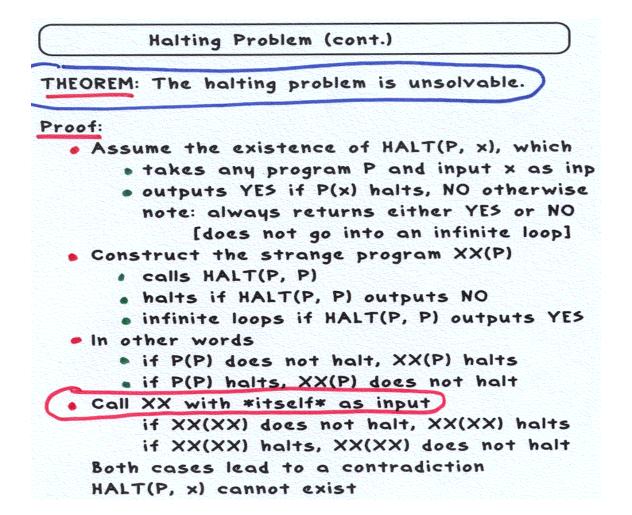


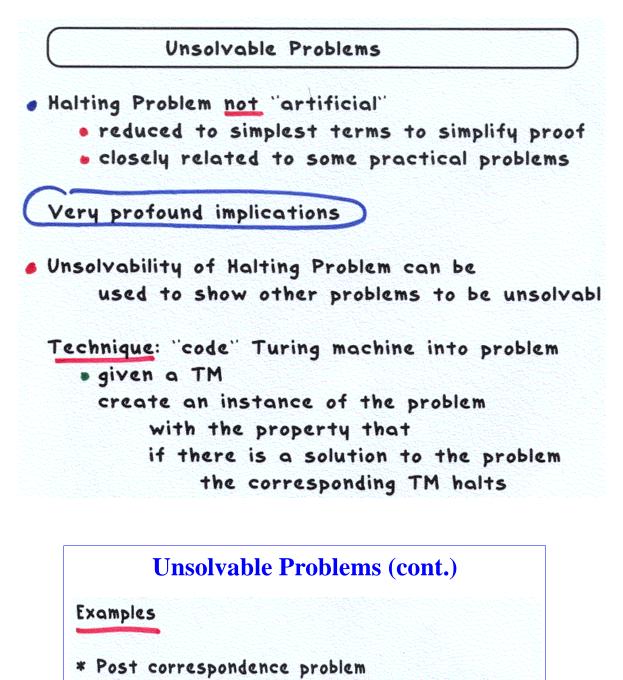












- * Do two programs produce the same output?
- * Hilbert's Tenth Problem (see next slide)
- * Equivalence of context-free grammars
- * Optimal data compression

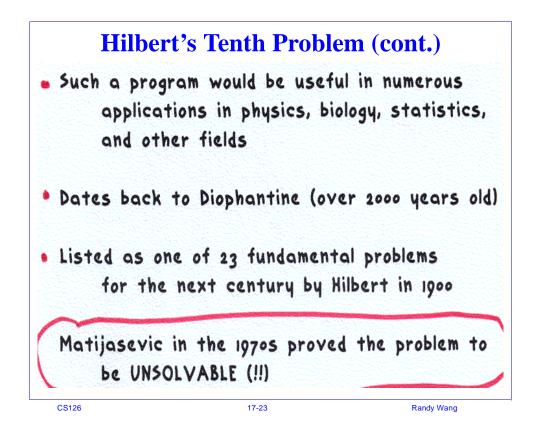
(shortest program to output a given string)

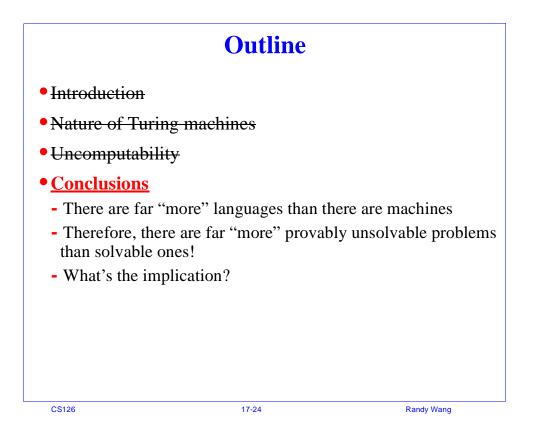
Randy Wang

Hilbert's Tenth Problem

Write a program to test whether a given multivariate polynomial has an integral root

Example 1: $6x^{3}yz^{2} + 3xy^{2} - x^{3} - 10$ YES: x = 5, y = 3, z = 0. Example 2: $x^{2} + y^{2} - 3$ NO.





(Implications
Practi	cal
• W	ork with limitations
	recognize and avoid unsolvable problems
• le	arn from structure
	same theory tells us about efficiency
Philoso	phical
(c	aveat: ask a philosopher)
• w	e "assume" that step-by-step reasoning
	will solve *any* scientific or technical
	problem
🔹 🕘 `'n	ot quite" says the halting problem
• ar	lything that "is like" (could be) a computer
	has the same flaw
	• physical machine (rods/gears, etc.)
	• human brain?
	matter itself?
	o universe?