# CS 126 Lecture A3: Boolean Logic

# Outline

## • Introduction

• Logic gates

• Boolean algebra

• Implementing gates with switching devices

• Common combinational devices

Conclusions

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### **Defining a Boolean Function with** a Truth Table 0 1 1 0 х 1 0 1 0 У AND(x,y)1 0 0 0 • A systematic way of specifying a function value for <u>all</u> possible combination of input values • A function that takes 2 inputs has 2x2 columns • A function that takes n inputs has 2<sup>n</sup> columns

• This particular example is the AND-function

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x	0	0	1	1
У	0	1	0	
OR(x,y)	0	1	1	1
	x	0	1	]
NO	T(x)	1	0	

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x	0	0	1	1	
У	0	1	0	1	
$XOR(x,y)=x^y$	0	1	1	0	
XOR(x,y) = 2 We have learned that any	<b>k^y =</b>	<b>x'y</b> can be	<b>+ x</b> defined	<b>Y</b> ' in thes	

			. 1		
0	0	1	1	× all fu	nctions of two variable
0	1	0	1	into o	one table
0	0	0	0	constant 0	
0	0	0	1	AND (xy) [	decode 11 = 3]
0	0	1	0	1	decode 10 = 2]
0	0	1	1	x	
0	1	0	0	C	decode 01 = 1]
0	1	0	1	У	
0	1	1	0	XOR (x^y)	
0	1	1	1	OR (x+y)	
1	0	0	0	NOR ("not or") [	decode 00 = 0]
1	0	0	1	== ("not xor")	East an and a block the set
1	0	1	0	NOT y (y')	For n variables, there
1	0	1	1		are a total of
1	1	0	0	NOT x (x')	$\sim 2^{n}$
1	1	0	1		
1	1	1	0	NAND ("not and")	functions!
1	1	1	1	constant 1	













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<b>Deriving D</b>	ecod	er I	Bool	lean	Ex	pre	ssio	ns	
x	0	0	0	0	1	1	1	1	
У	0	0	1	1	0	0	1	1	
Z	0	1	0	1	0	1	0	1	
d <sub>0</sub>	1	0	0	0	0	0	0	0	
d <sub>0</sub> =x'y'z'									
x	0	0	0	0	1	1	1	1	
У	0	0	1	1	0	0	1	1	
Z	0	1	0	1	0	1	0	1	
d <sub>1</sub>	0	1	0	0	0	0	0	0	
		d <sub>1</sub> =x	'y'z	i					
• Can bypass truth	table	when	n you	're co	omfo	rtable	e with	ı this	
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# **Building a Computer Bottom Up Circuit design**: specifying the interconnection of components such as resistors, diodes, and transistors to form logic building blocks **Logic design**: determining how to interconnect logic building blocks such as logic gates and flip-flops to form subsystems **System design** (or computer architecture): specifying the number, type, and interconnection of subsystems such as memory units, ALUs, and I/O devices

# What We Have Learned • How to build basic gates using transistors • How to build a combinational circuit - Truth table - Sum-of-product boolean expression - Transform a boolean expression into a circuit of basic gates • The functionality of some common devices and how they are made - Decoder - Multiplexer - Bit-slice adder • You're <u>not</u> responsible for - Boolean algebra laws, or circuit simplification CS126 11-42 Randy Wang