

CS 126 Lecture A1: TOY Machine

Outline

- **Introduction**
- Toy machine
- Machine language instructions
- Example machine language programs
- Conclusions

Brief History Leading to the Dominance of von Neumann Architecture

- 1940s, Atanasoff, Iowa State, first **special-purpose** electronic computer, binary representation of numbers
- ~1946, ENIAC, Eckert and Mauchly, UPenn, first general-purpose electronic computer
 - 100 ft long, 8.5 ft high, several ft wide, 18000 vacuum tubes
 - conditional jumps, **programmable**
 - code: setting switches, data: punch cards
 - Used to compute artillery firing tables
- 1944, von Neumann, visited ENIAC, the “**von Neumann Memo**”, concept of a “stored-program” computer
- 1949, Wilkes, EDSAC, first **stored-program** computer
- 1946, von Neumann, Goldstine, Burks, IAS machine, Princeton, the report pioneered most modern computer architecture concepts

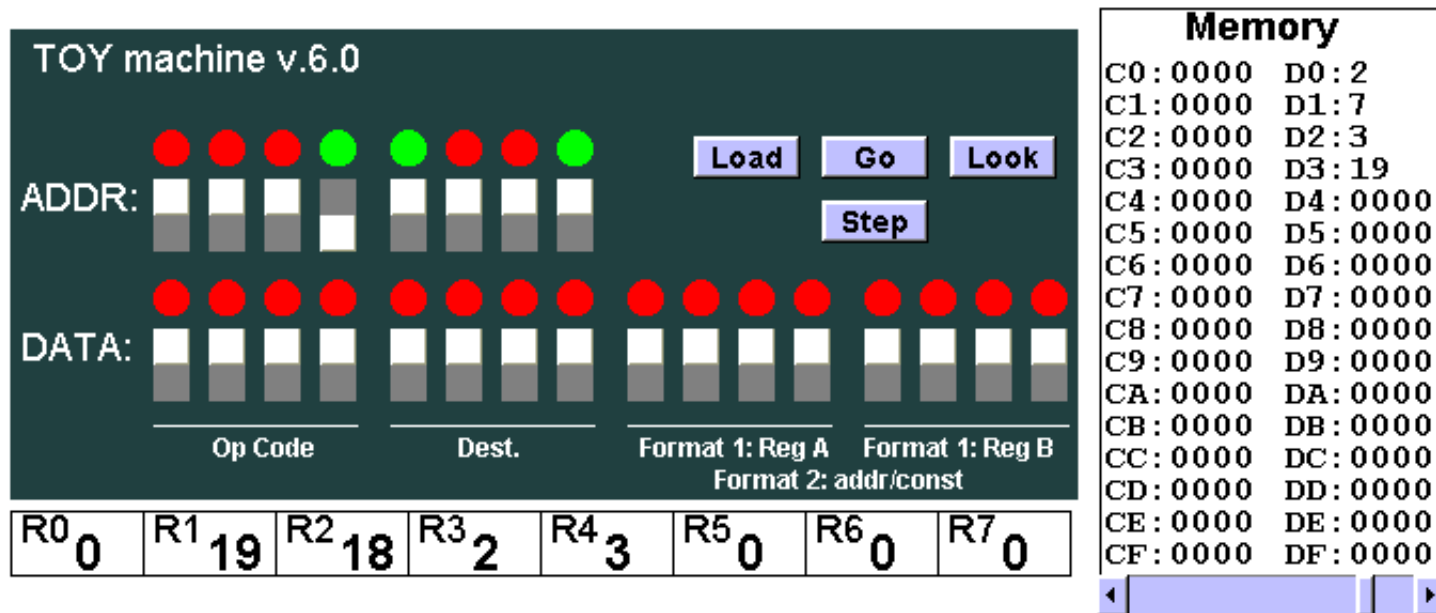
Why Study Machine Language Programming Today

- Learn how computers really work
- There are still (a few) situations where machine language programming is necessary
- The first step towards understanding how to build better computers

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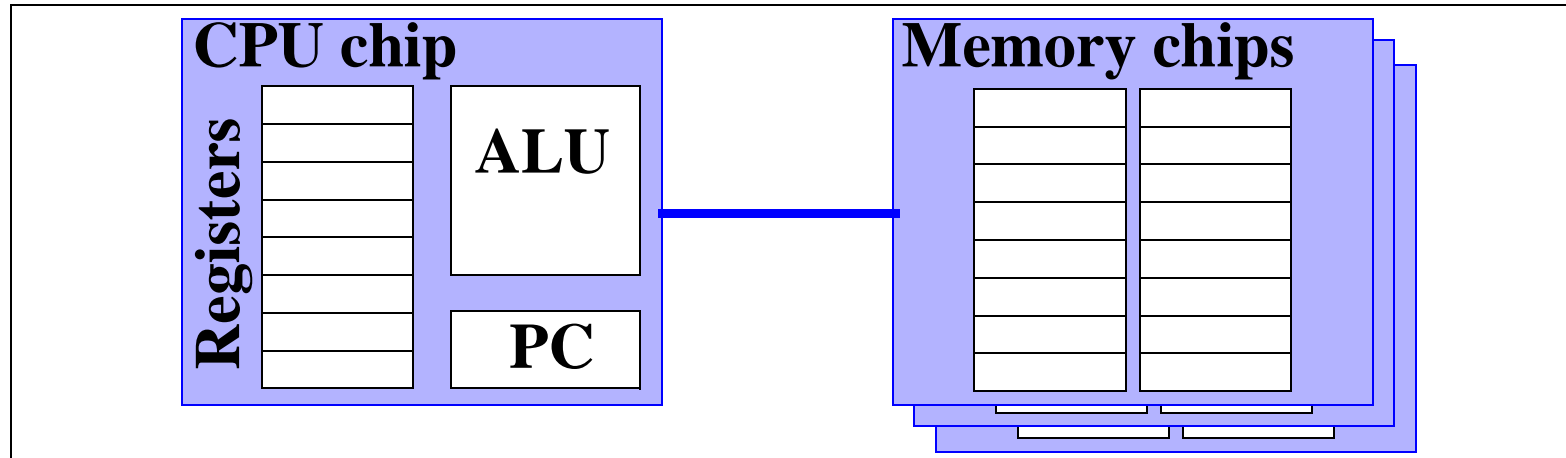
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Toy Machine



- An imaginary machine, similar to
 - * ancient early computers
 - * today's microprocessors
- Box with switches and lights, maybe TTY

Inside the Box



- ALU (arithmetic logic unit) -- executes instructions to manipulate data
- 8 registers -- the fastest form of storage, on-chip in modern computers, used as scratch space during computation
- PC (program counter) -- a register with special meaning, keeps track of the next instruction to be executed
- 256 16-bit words of memory -- stores both code and data

Binary Numbers

- Machine consists of two-state ("ON-OFF") switches and lights
- Use binary encoding to represent values

Ex:

integers

$$.6375 = 0001100011100111$$

. 15 14 13 12 11 10 9 8 7 6 5 4 3 2 1 0

. 0 0 0 1 1 0 0 0 1 1 1 0 0 1 1 1

. 12 11 7 6 5 2 1 0
 . 2 + 2 2 + 2 + 2 2 + 2 + 2

$$.6375 = 4096 + 2048 \qquad +128 + 64 + 32 \qquad +4 + 2 + 1$$

Hexadecimal Numbers

- Hexadecimal (base-16) notation provides shorthand binary code four bits at a time

0000	0001	0010	0011	0100	0101	0110	0111
0	1	2	3	4	5	6	7
1000	1001	1010	1011	1100	1101	1110	1111
8	9	A	B	C	D	E	F

Ex:

$$\begin{array}{cccc} \cdot & 6375 & = & 0001100011100111 \\ & & & \hline & & & 1 \quad 8 \quad E \quad 7 \end{array}$$

$$\begin{array}{l} \cdot \\ \cdot \\ \cdot \end{array} \quad 6375 = 1 \cdot 16^3 + 8 \cdot 16^2 + 14 \cdot 16^1 + 7 \cdot 16^0$$
$$\cdot \quad = 4096 + 2048 + 224 + 7$$

TOY machine memory

Contents of machine in hexadecimal ("dump")

PC: 0010

R0: R1: R2: R3: R4: R5: R6: R7:
0000 0788 B700 0010 0401 0002 0003 00A0

00:	0000	0000	0000	0000	0000	0000	0000	0000	0000
08:	0000	0000	0000	0000	0000	0000	0000	0000	0000
10:	9222	9120	1121	A120	1121	A121	7211	0000	16
18:	0000	0001	0002	0003	0004	0005	0006	0007	
20:	0008	0009	000A	000B	000C	000D	000E	000F	
28:	0000	0000	0000	FE10	FACE	CAFE	ACED	CEDE	
.									
.									
E8:	1234	5678	9ABC	DEF0	0000	0000	F00D	0000	EE
F0:	0000	0000	EEEE	1111	EEEE	1111	0000	0000	
F8:	B1B2	F1F5	0000	0000	0000	0000	0000	0000	

- Programmers still look at dumps, even today
- Contents of memory
 - record of what program has done
 - determines (with PC) what machine will do

Program and Data

Program: sequence of instructions

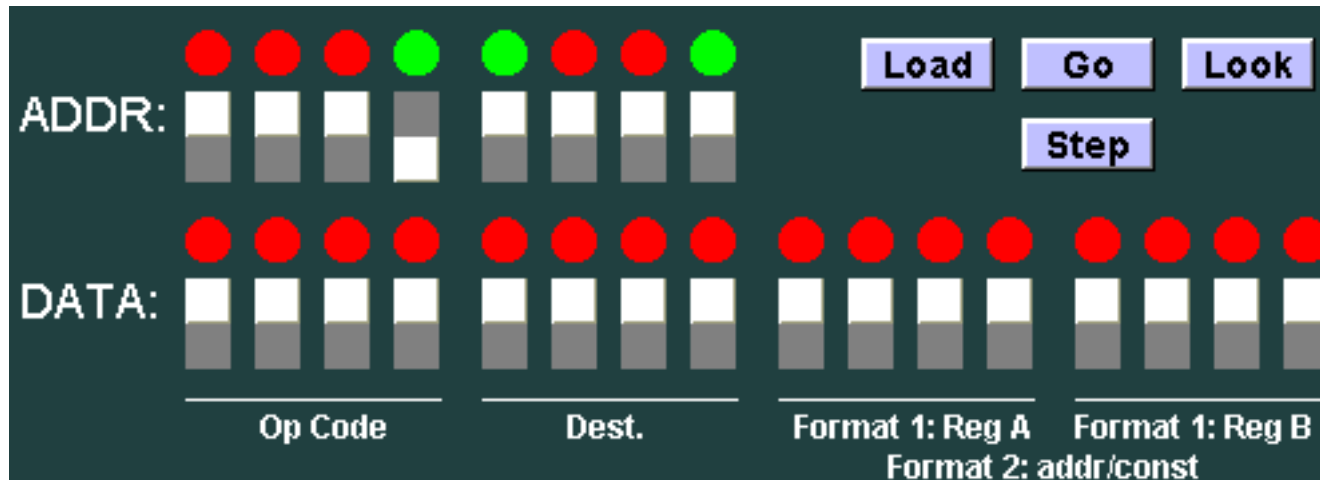
Instruction:

16-bit word (interpreted one way)

Data:

16-bit word (interpreted other ways)

How to Use the TOY Machine



To run a program

- * load the program and data

(set switches, press LOAD for each word)

- * set switches to address of first instruction

- * press GO

How to Use the TOY Machine

GO button

- * loads PC from address switches
- * initiates FETCH-INCREMENT-EXECUTE cycle
- * machine runs until halt instruction hit

FETCH (get instruction from memory into CPU)

INCREMENT program counter (PC)

EXECUTE (may require data from or to memory)

Output:

- read contents of memory word in lights
- system call can write output to an output device (tty)

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TOY Instructions

0:	halt	
1:	add	} arithmetic
2:	subtract	
3:	multiply	
4:	system call	} control flow
5:	jump	
6:	jump if greater	
7:	jump and count	
8:	jump and link	} memory
9:	load	
A:	store	
B:	load address	} logic
C:	xor	
D:	and	
E:	shift right	
F:	shift left	

- Encode each of these instructions using 16 bits
- Need to divide up the 16 bits to denote components of each type of instructions
- Instruction formats - different ways of dividing up the 16 bits

Instruction Format 1

FORMAT 1: register-register

4 bits	4 bits	4 bits	4 bits
opcode	dest	regA	regB

Ex: 1234 means

add register R3 and R4

put the result in R2

$$R_2 \leftarrow R_3 + R_4$$

Other instrs: sub, mult, xor, and

Instruction Format 2

FORMAT 2: register-memory, register-immediate

4 bits	4 bits	8 bits
opcode	dest	addr/const

Ex: 9234 means "load memory loc 34 (hex) into R2"

R2 ← mem[34]

Ex: A234 means "store R2 into memory loc 34"

mem[34] ← R2

Ex: B234 means "load the value 0034 into R2"

R2 ← 0034

Other instrs: shifts, halt, system call, jumps

Logical Instructions

opcode

C: xor
D: and
E: shift right
F: shift left

xor, and: bit-by-bit operations
shift: move bits

Right-Shift

X

100101	0110000011
--------	------------

discarded

0-filled

0000000000	100101
------------	--------

X >> 10

Bit-by-Bit-And

1	0	0	1	0	1	0	1	1	0	0	0	0	0	1	0	a
0	0	1	1	0	0	1	0	1	0	1	1	0	0	1	1	b
0	0	0	1	0	0	1	0	1	0	0	0	0	0	1	0	a&b

MASKING with "and instruction"

a	1010010x01111010
b	0000000100000000
a&b	00000000x00000000

Other Logical Operations

- Can implement other logical operations

a	b	and	xor	or
		&	^	(a & b) ^ (a ^ b)
0	0	0	0	0
0	1	0	1	1
1	0	0	1	1
1	1	1	0	1

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Sample TOY program o: arithmetic

Ex: TOY code for C expression $t = b*b - 4*a*c$
memory loc Do is used for storing a

D1 for b

D2 for c

D3 for t

• Suppose memory locations 10-19 contain

10: 91D1 3111 B204 93D0 94D2 3223 3224 2112
18: A1D3 0000

• Set PC to 10; Press GO. TOY computes the value.

• Step-by-step trace:

10: 91D1 R1 ← b
11: 3111 R1 ← b*b
12: B204 R2 ← 4
13: 93D0 R3 ← a
14: 94D2 R4 ← c
15: 3223 R2 ← 4*a
16: 3224 R2 ← (4*a)*c
17: 2112 R2 ← (b*b) - (4*a*c)
18: A1D3 t ← (b*b - 4*a*c)
19: 0000 halt

TOY Demo

TOY machine v.6.0

ADDR: ● ● ● ● ● ● ● ●

DATA: ● ● ● ● ● ● ● ● ● ● ● ● ● ●

Op Code Dest. Format 1: Reg A Format 1: Reg B
Format 2: addr/const

Load Go Look

Step

R0	0	R1	31	R2	4	R3	2	R4	3	R5	0	R6	0	R7	0
----	---	----	----	----	---	----	---	----	---	----	---	----	---	----	---

Memory			
10:	91D1	20:	0000
11:	3111	21:	0000
12:	B204	22:	0000
13:	93D0	23:	0000
14:	94D2	24:	0000
15:	3223	25:	0000
16:	3224	26:	0000
17:	2112	27:	0000
18:	A1D3	28:	0000
19:	0000	29:	0000
1A:	0000	2A:	0000
1B:	0000	2B:	0000
1C:	0000	2C:	0000
1D:	0000	2D:	0000
1E:	0000	2E:	0000
1F:	0000	2F:	0000

Mem: 10 Reload From HTML

Data: 0000 Load From HTML

Current Instruction
15:3223 Multiply
R2=R2*R3

Sample TOY program i: more arithmetic

Ex: Suppose memory locations 10-1F contain

10: B001 B200 B101 1221 1110 1221 1110 1221
18: 1110 1221 1110 1221 1110 1221 1110 0000 0000

● Set PC to 10. Press GO. What happens?

● Step-by-step trace:

10:	B001	R0	<-	0001				
11:	B200	R2	<-	0000				0000
12:	B101	R1	<-	0001			0001	
13:	1221	R2	<-	R2 + R1				0001
14:	1110	R1	<-	R1 + R0		0002		
15:	1221	R2	<-	R2 + R1				0003
16:	1110	R1	<-	R1 + R0		0003		
17:	1221	R2	<-	R2 + R1				0006
18:	1110	R1	<-	R1 + R0		0004		
19:	1221	R2	<-	R2 + R1				000A
1A:	1110	R1	<-	R1 + R0		0005		
1B:	1221	R2	<-	R2 + R1				000F
1C:	1110	R1	<-	R1 + R0		0006		
1D:	1221	R2	<-	R2 + R1				0015
1E:	0000			halt				

Computes $1 + 2 + 3 + 4 + 5 + 6 = 21$

Sample TOY program 2: loop

- Suppose memory locations 10-17 contain
10: B106 B200 B001 1221 2110 6113 0000 0000
- Set PC to 10. Press GO. What happens?
- Step-by-step trace:

10:	B106	R1 ← 0006	0006	sum
11:	B200	R2 ← 0000	0000	
12:	B001	R0 ← 0001		
13:	1221	R2 ← R2 + R1	0006	
14:	2110	R1 ← R1 - R0	0005	
15:	6113	jump if (R1 > 0)		
13:	1221	R2 ← R2 + R1	000B	
14:	2110	R1 ← R1 - R0	0004	
15:	6113	jump if (R1 > 0)		
13:	1221	R2 ← R2 + R1	000F	
14:	2110	R1 ← R1 - R0	0003	
15:	6113	jump if (R1 > 0)		
13:	1221	R2 ← R2 + R1	0012	
14:	2110	R1 ← R1 - R0	0002	
15:	6113	jump if (R1 > 0)		
13:	1221	R2 ← R2 + R1	0014	
14:	2110	R1 ← R1 - R0	0001	
15:	6113	jump if (R1 > 0)		
13:	1221	R2 ← R2 + R1	0015	
14:	2110	R1 ← R1 - R0	0000	
15:	6113	jump if (R1 > 0)		
16:	0000	halt		

Computes

$$N + (N-1) + \dots + 3 + 2 + 1 = N(N+1)/2$$

for *any* value N loaded into R1

Horner's Method

Problem:

- evaluate $2x^3 + 3x^2 + 9x + 7$ at $x = 10$
assume "data" stored in locations 30--34

x a b c d

30: 000A 0002 0003 0009 0007 0000 0000 0000

First try:

- compute x^3 , mult. by a; compute x^2 , ...
(cumbersome, inefficient)
- Efficient algorithm (Horner's method):
rewrite $ax^3 + bx^2 + cx + d$ as $((ax + b)x + c)x + d$

Sample TOY Program 3: Horner's Method

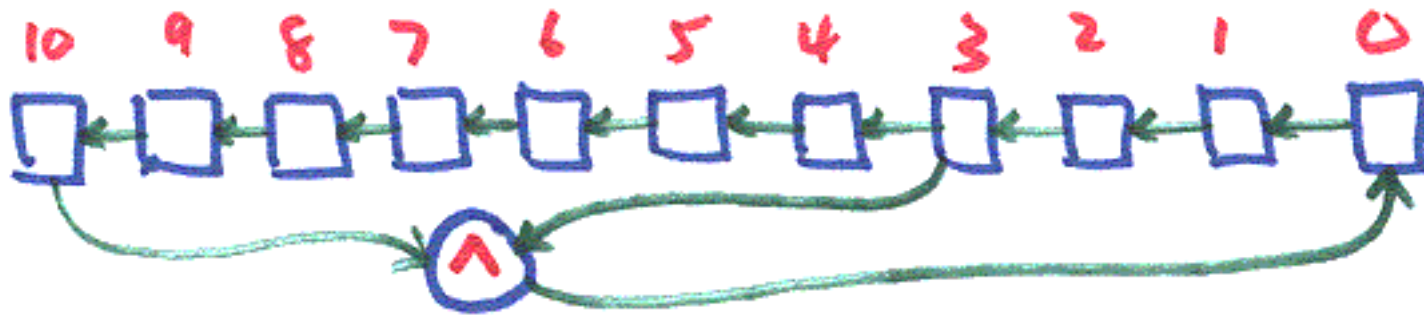
- Efficient algorithm (Horner's method):

rewrite ax^3+bx^2+cx+d as $((ax+b)x+c)x+d$

```
10: 9430 R4 <- M[30]      000A x
11: 9531 R5 <- M[31]      0002 a
12: 3554 R5 <- R5 * R4    0014 a*x
13: 9632 R6 <- M[32]      0003 b
14: 1556 R5 <- R5 + R6    0017 a*x+b
15: 3554 R5 <- R5 * R4    00DC (a*x+b)*x
16: 9633 R6 <- M[33]      0009 c
17: 1556 R5 <- R5 + R6    00E5 (a*x+b)*x + c
18: 3554 R5 <- R5 * R4    0956 ((a*x+b)*x+c)*x
19: 9634 R6 <- M[34]      0007 d
1A: 1556 R5 <- R5 + R6    095D ((a*x+b)*x+c*x)+d
1B: 4502 write R5 to tty
```

LFBSR

Linear feedback shift register (LFBSR)



Sample TOY program 4: bit manipulation

Ex: suppose that memory locations 10-15 contain

10: 911F B000 1210 1310 E203 E30A C323 B401

18: D334 F101 C113 0000 0000 0000 0000 0684

• Set PC to 10. Press GO. What happens?

• Step-by-step:

10:	911F	R1 <- 0684	0000011010000100	R1 is LFBSR content
11:	B000	R0 <- 0000		
12:	1210	R2 <- R1 + R0	0000011010000100	R2 is a copy of R1
13:	1310	R3 <- R1 + R0	0000011010000100	So is R3
14:	E203	R2 <- R2 >> 3	0000000011010000	Get 3rd bit to the right end
15:	E30A	R3 <- R3 >> 10	0000000000000001	Get 10th bit to the right end
16:	C323	R3 <- R2 ^ R3	0000000011010001	Only right-most bit of xor
17:	B401	R4 <- 0001	0000000000000001	
18:	D334	R3 <- R3 & R4	0000000000000001	
19:	F101	R1 <- R1 << 1	0000110100001000	Left shift LFBSR
1A:	C113	R1 <- R1 ^ R3	0000110100001001	Put in the new right-most bit
1B:	0000	halt		

• Simulates one step of LFBSR of Lecture 1

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Basic Characteristics of TOY Machine

TOY is a "general purpose" computer

- "von Neumann" machine
 - instructions and data in same memory
 - can change program (control) w/o rewiring
 - immediate applications
 - profound implications
- sufficient power to perform any computation
 - limited only by amount of memory (and time)
[stay tuned]
- similar to real machines

“Computer Architecture”

Compilers

Machine language programmers



Instruction Set Architecture: instruction set, registers, memory

Implementation: “Organization” and “Hardware”

“Computer Architecture”

- Interface--“instruction set architecture” (ISA)
 - visible to machine language programmers
 - boundary between software and hardware
- Implementation
 - “Organization”: interaction of high-level components
 - “Hardware”: low level specifics such as detailed logic design
- Abstractions
 - Can change hardware without changing organization
 - Can change implementation without changing ISA